Data Structures

Version 5.0.2

November 6, 2010

(require data)

This manual documents data structure libraries available in the data collection.

1 Imperative Queues

```
(require data/queue)
```

This module provides a simple mutable queue representation, first-in/first-out only. Operations on queues mutate it in a thread-unsafe way.

```
(make-queue) → queue/c
```

Produces an empty queue.

```
 \begin{array}{c} (\text{enqueue!} \ q \ v) \ \rightarrow \ \text{void?} \\ q : \text{queue/c} \\ v : \text{any/c} \end{array}
```

Adds an element to the back of a queue.

Removes an element from the front of a nonempty queue, and returns that element.

Examples:

```
(define q (make-queue))
> (enqueue! q 1)
> (dequeue! q)
1
> (enqueue! q 2)
> (enqueue! q 3)
> (dequeue! q)
2
> (dequeue! q)
3
```

```
(queue-empty? q) \rightarrow boolean? q: queue/c
```

Recognizes whether a queue is empty or not.

Examples:

```
(define q (make-queue))
> (queue-empty? q)
#t
```

```
> (enqueue! q 1)
> (queue-empty? q)
#f
> (dequeue! q)
1
> (queue-empty? q)
#t

(queue? v) → boolean?
v : any/c

This predicate recognizes queues.

Examples:
> (queue? (make-queue))
#t
> (queue? 'not-a-queue)
#f

queue/c : flat-contract?
```

These contracts recognize queues; the latter requires the queue to contain at least one value.

nonempty-queue/c : flat-contract?

2 Growable Vectors

```
(require data/gvector)
```

A growable vector (gvector) is a mutable sequence whose length can change over time. A gvector also acts as a dictionary (dict? from racket/dict), where the keys are zero-based indexes and the values are the elements of the gvector. A gvector can be extended by adding an element to the end, and it can be shrunk by removing any element, although removal can take time linear in the number of elements in the gvector.

Two gvectors are equal? if they contain the same number of elements and if the contain equal elements at each index.

```
(make-gvector [#:capacity capacity]) → gvector?
capacity : exact-positive-integer? = 10
```

Creates a new empty gvector with an initial capacity of capacity.

```
(gvector elem ...) → gvector?
elem : any/c
```

Creates a new gvector containing each elem in order.

```
(gvector? x) → boolean?
x : any/c
```

Returns #t if x is a gvector, #f otherwise.

```
(gvector-ref gv index [default]) → any/c
  gv : gvector?
  index : exact-nonnegative-integer?
  default : any/c = (error ....)
```

Returns the element at index index, if index is less than (gvector-count gv). Otherwise, default is invoked if it is a procedure, returned otherwise.

```
(gvector-add! gv value ...) → void?
  gv : gvector?
  value : any/c
```

Adds each value to the end of the gvector gv.

Sets the value at index index to be value. If index is (gvector-count gv)—that is, one more than the greatest used index—the effect is the same as (gvector-add! gv value).

Removes the item at *index*, shifting items at higher indexes down. Takes time proportional to (- (gvector-count gv) index).

```
(gvector-count \ gv) \rightarrow exact-nonnegative-integer? \ gv : gvector?
```

Returns the number of items in gv.

```
(gvector->vector gv) → vector?
gv : gvector?
```

Returns a vector of length (gvector-count gv) containing the elements of gv in order.

```
(in-gvector gv) → sequence?
gv : gvector?
```

Returns a sequence whose elements are the elements of gv. Mutation of gv while the sequence is running changes the elements produced by the sequence. To obtain a sequence from a snapshot of gv, use (in-vector (gvector->vector gv)) instead.

```
(for/gvector (for-clause ...) body ...+)
(for*/gvector (for-clause ...) body ...+)
```

Analogous to for/list and for*/list, but constructs a gvector instead of a list.

Unlike for/list, the *body* may return zero or multiple values; all returned values are added to the gyector, in order, on each iteration.

3 Orders and Ordered Dictionaries

```
(require data/order)
```

This library defines orders and the ordered dictionary generic interface.

```
ordering/c : flat-contract?
```

Contract for orderings, represented by the symbols '=, '<, and '>.

Struct-type property for defining new ordered dictionary types. The value associated with prop:ordered-dict should be an immutable vector of six procedures, two "extrema" procedures and four "search" procedures. The extrema procedures must satisfy e/c and the search procedures must satisfy s/c:

The procedures are implementations of the following generic functions:

- dict-iterate-least
- dict-iterate-greatest
- dict-iterate-least/>?
- dict-iterate-least/>=?
- dict-iterate-greatest/<?
- dict-iterate-greatest/<=?

A struct type that implements prop:ordered-dict must also implement prop:dict.

```
(ordered-dict? x) → boolean?
x : any/c
```

Returns #t if x is an instance of a struct implementing the ordered dictionary interface (via prop:ordered-dict).

```
(dict-iterate-least dict) → any/c
  dict : ordered-dict?
(dict-iterate-greatest dict) → any/c
  dict : ordered-dict?
```

Returns the position of the least (greatest) key in the ordered dictionary dict. If dict is empty, #f is returned.

```
(dict-iterate-least/>? dict key) → any/c
  dict : ordered-dict?
  key : any/c
(dict-iterate-least/>=? dict key) → any/c
  dict : ordered-dict?
  key : any/c
(dict-iterate-greatest/<? dict key) → any/c
  dict : ordered-dict?
  key : any/c
(dict-iterate-greatest/<=? dict key) → any/c
  dict : ordered-dict?
  key : any/c</pre>
```

Returns the position of the least key greater than key, the least key greater than or equal to key, the greatest key less than key, and the greatest key less than or equal to key, respectively. If no key satisfies the criterion, #f is returned.

```
(order name domain-contract comparator)
  → (and/c order? procedure?)
  name : symbol?
  domain-contract : contract?
  comparator : (-> any/c any/c ordering/c)
(order name domain-contract =? <? [>?]) → (and/c order? procedure?)
  name : symbol?
  domain-contract : contract?
  =? : (-> any/c any/c boolean?)
  <? : (-> any/c any/c boolean?)
  >? : (-> any/c any/c boolean?) = (lambda (x y) (<? y x))</pre>
```

Produces a named order object encapsulating a domain contract and a comparator function. If a single procedure is given, it is used directly as the comparator. If two or three procedures are given, they are used to construct the comparator.

The domain-contract is not applied to the comparison function; rather, clients of the order are advised to incorporate the domain contracts into their own contracts. For example, when

a splay-tree (see data/splay-tree) is constructed with an order, it applies the domain-contract to its keys. Thus the contract is checked once per dictionary procedure call, rather than on every comparison.

An order object is applicable as a procedure; it behaves as its comparator.

Examples:

```
> (define string-order (order 'string-order string? string=? string<?))
> (string-order "abc" "acdc")
'<
> (string-order "x" 12)
string=?: expects type < string> as 2nd argument, given: 12;
other arguments were: "x"
```

```
(order? x) → boolean?
  x : any/c
```

Returns #t if x is an order object, #f otherwise.

```
(order-comparator ord) → (-> any/c any/c ordering/c)
  ord : order?
```

Extracts the comparator function from an order object.

```
(order-domain-contract ord) → contract?
ord : order?
```

Extracts the domain contract from an order object.

```
(order-=? ord) → (-> any/c any/c boolean?)
  ord : order?
(order-<? ord) → (-> any/c any/c boolean?)
  ord : order?
```

Returns a procedure representing the order's equality relation or less-than relation, respectively.

```
real-order : order?
```

The order of the real numbers. The domain of real-order excludes +nan.0 but includes +inf.0 and -inf.0. The standard numeric comparisons (=, <) are used; exact 1 is equal to inexact 1.0.

Examples:

```
> (real-order 1.0 1)
'=
> (real-order 5 7)
'<
> (real-order 9.0 3.4)
'>
> (real-order 1 +inf.0)
'<
> (real-order 5 -inf.0)
'>
```

datum-order : order?

An ad hoc order that encompasses many built-in Racket data types. The datum-order comparator orders values of the same data type according to the data type's natural order: string=?, string<? for strings, for example (but see the warning about numbers below). Different data types are ordered arbitrarily but contiguously; for example, all strings sort before all vectors, or vice versa. Programs should not rely on the ordering of different data types.

The order is designed so that lists, vectors, and prefab structs are ordered lexicographically.

Warning! The datum-order is not compatible with the standard numeric order; all exact numbers are ordered before all inexact numbers. This allows 1 to be considered distinct from 1.0, for example.

The following built-in data types are currently supported: numbers, strings, bytes, keywords, symbols, booleans, characters, null, pairs, vectors, boxes, and prefab structs.

Examples:

```
> (datum-order 1 2)
'<
> (datum-order 8 5.0)
'<
> (datum-order 3+5i 3+2i)
'>
> (datum-order '(a #:b c) '(a #:c d c))
'<
> (datum-order "apricot" "apple")
'>
> (datum-order '#(1 2 3) '#(1 2))
'>
> (datum-order '#(1 2 3) '#(1 3))
'<
> (datum-order 'apple (box "candy"))
```

4 Splay Trees

```
(require data/splay-tree)
```

Splay trees are an efficient data structure for mutable dictionaries with totally ordered keys. They were described in the paper "Self-Adjusting Binary Search Trees" by Daniel Sleator and Robert Tarjan in Journal of the ACM 32(3) pp652-686.

A splay-tree is a ordered dictionary (dict? and ordered-dict?).

Makes a new empty splay-tree. The splay tree uses ord to order keys; in addition, the domain contract of ord is combined with key-contract to check keys.

Examples:

```
> (define splay-tree
    (make-splay-tree (order 'string-order string? string=? string<?)))</pre>
> (splay-tree-set! splay-tree "dot" 10)
> (splay-tree-set! splay-tree "cherry" 500)
> (dict-map splay-tree list)
'(("cherry" 500) ("dot" 10))
> (splay-tree-ref splay-tree "dot")
> (splay-tree-remove! splay-tree "cherry")
> (splay-tree-count splay-tree)
1
> (splay-tree-set! splay-tree 'pear 3)
<collects>/data/splay-tree.rkt:1112.2: top-level broke the
contract
  (->i
  ((s splay-tree?) (key (s) ...) (v (s) ...))
on splay-tree-set!; expected <string?>, given: 'pear
```

```
value-contract : contract? = any/c
```

Makes a new empty splay-tree that permits only exact integers as keys (in addition to any constraints imposed by key-contract). The resulting splay tree answers true to adjustable-splay-tree? and supports efficient key adjustment.

Examples:

```
> (define splay-tree (make-adjustable-splay-tree))
> (splay-tree-set! splay-tree 3 'apple)
> (splay-tree-set! splay-tree 6 'cherry)
> (dict-map splay-tree list)
'((3 apple) (6 cherry))
> (splay-tree-ref splay-tree 3)
'apple
> (splay-tree-remove! splay-tree 6)
> (splay-tree-count splay-tree)
1
```

```
(splay-tree? x) \rightarrow boolean? x : any/c
```

Returns #t if x is a splay-tree, #f otherwise.

```
(adjustable-splay-tree? x) → boolean?
x : any/c
```

Returns #t if x is a splay-tree that supports key adjustment; see splay-tree-contract! and splay-tree-expand!.

```
(splay-tree-ref s key [default]) → any
  s : splay-tree?
  key : any/c
  default : any/c = (lambda () (error ....))
(splay-tree-set! s key value) → void?
  s : splay-tree?
  key : any/c
  value : any/c
(splay-tree-remove! s key) → void?
  s : splay-tree?
  key : any/c
(splay-tree-count s) → exact-nonnegative-integer?
  s : splay-tree?
(splay-tree-iterate-first s) → (or/c #f splay-tree-iter?)
  s : splay-tree?
```

```
(splay-tree-iterate-next s iter) → (or/c #f splay-tree-iter?)
s : splay-tree?
iter : splay-tree-iter?
(splay-tree-iterate-key s iter) → any/c
s : splay-tree?
iter : splay-tree-iter?
(splay-tree-iterate-value s iter) → any/c
s : splay-tree?
iter : splay-tree?
iter : splay-tree.
```

Implementations of dict-ref, dict-set!, dict-remove!, dict-count, dict-iterate-first, dict-iterate-next, dict-iterate-key, and dict-iterate-value, respectively.

```
(splay-tree-remove-range! s from to) → void?
s : splay-tree?
from : any/c
to : any/c
```

Removes all keys in [from, to); that is, all keys greater than or equal to from and less than to.

This operation takes O(N) time, or $O(\log N)$ time if (adjustable-splay-tree? s).

```
(splay-tree-contract! s from to) → void?
s : adjustable-splay-tree?
from : exact-integer?
to : exact-integer?
```

Like splay-tree-remove-range!, but also decreases the value of all keys greater than or equal to to by (- to from).

This operation is only allowed on adjustable splay trees, and it takes $O(\log N)$ time.

```
(splay-tree-expand! s from to) → void?
s : adjustable-splay-tree?
from : exact-integer?
to : exact-integer?
```

Increases the value of all keys greater than or equal to from by (- to from).

This operation is only allowed on adjustable splay trees, and it takes $O(\log N)$ time.

```
(splay-tree-iterate-least s) \rightarrow (or/c #f splay-tree-iter?)
  s : splay-tree
(splay-tree-iterate-greatest s) \rightarrow (or/c #f splay-tree-iter?)
  s : splay-tree
(splay-tree-iterate-least/>? s key) \rightarrow (or/c #f splay-tree-iter?)
  s : splay-tree?
  key : any/c
(splay-tree-iterate-least/>=? s key)
→ (or/c #f splay-tree-iter?)
 s : splay-tree?
  key : any/c
(splay-tree-iterate-greatest/<? s key)</pre>
→ (or/c #f splay-tree-iter?)
 s : splay-tree?
  key: any/c
(splay-tree-iterate-greatest/<=? s key)</pre>
 → (or/c #f splay-tree-iter?)
 s : splay-tree?
  key : any/c
```

Implementations of dict-iterate-least, dict-iterate-greatest, dict-iterate-least/>?, dict-iterate-least/>=?, dict-iterate-greatest/<?, and dict-iterate-greatest/<=?, respectively.

```
(splay-tree-iter? x) → boolean?
x : any/c
```

Returns #t if x represents a position in a splay-tree, #f otherwise.

Returns an association list with the keys and values of s, in order.

5 Skip Lists

```
(require data/skip-list)
```

Skip lists are a simple, efficient data structure for mutable dictionaries with totally ordered keys. They were described in the paper "Skip Lists: A Probabilistic Alternative to Balanced Trees" by William Pugh in Communications of the ACM, June 1990, 33(6) pp668-676.

A skip-list is an ordered dictionary (dict? and ordered-dict?). It also supports extensions of the dictionary interface for iterator-based search and mutation.

Makes a new empty skip-list. The skip-list uses ord to order keys; in addition, the domain contract of ord is combined with key-contract to check keys.

Examples:

```
> (define skip-list (make-skip-list real-order))
> (skip-list-set! skip-list 3 'apple)
> (skip-list-set! skip-list 6 'cherry)
> (dict-map skip-list list)
'((3 apple) (6 cherry))
> (skip-list-ref skip-list 3)
'apple
> (skip-list-remove! skip-list 6)
> (skip-list-count skip-list)
1
```

Makes a new empty skip-list that permits only exact integers as keys (in addition to any constraints imposed by <code>key-contract</code>). The resulting skip-list answers true to adjustable-skip-list? and supports key adjustment.

```
(skip-list? v) \rightarrow boolean?
```

```
v : any/c
```

Returns #t if v is a skip-list, #f otherwise.

```
(adjustable-skip-list? v) → boolean?
v : any/c
```

Returns #t if v is a skip-list that supports key adjustment; see skip-list-contract! and skip-list-expand!.

```
(skip-list-ref skip-list key [default]) \rightarrow any/c
  skip-list : skip-list?
  key : any/c
  default : any/c = (lambda () (error ....))
(skip-list-set! skip-list key value) \rightarrow void?
  skip-list : skip-list?
  key : any/c
  value : any/c
(skip-list-remove! skip-list key) \rightarrow void?
  skip-list : skip-list?
  key : any/c
(skip-list-count \ skip-list) \rightarrow exact-nonnegative-integer?
  skip-list : skip-list?
(skip-list-iterate-first skip-list) \rightarrow (or/c skip-list-iter? #f)
  skip-list : skip-list?
(skip-list-iterate-next skip-list iter)
→ (or/c skip-list-iter? #f)
  skip-list : skip-list?
  iter : skip-list-iter?
(skip-list-iterate-key skip-list iter) \rightarrow any/c
  skip-list : skip-list?
  iter : skip-list-iter?
(skip-list-iterate-value skip-list iter) \rightarrow any/c
  skip-list : skip-list?
  iter : skip-list-iter?
```

Implementations of dict-ref, dict-set!, dict-remove!, dict-count, dict-iterate-first, dict-iterate-next, dict-iterate-key, and dict-iterate-value, respectively.

```
(skip-list-remove-range! skip-list from to) \rightarrow void? skip-list: skip-list? from: any/c to: any/c
```

Removes all keys in [from, to); that is, all keys greater than or equal to from and less than to.

```
(skip-list-contract! skip-list from to) → void?
  skip-list : adjustable-skip-list?
  from : exact-integer?
  to : exact-integer?
```

Like skip-list-remove-range!, but also decreases the value of all keys greater than or equal to to by (- to from).

This operation takes time proportional to the number of elements with keys greater than or equal to to.

```
(skip-list-expand! skip-list from to) → void?
skip-list: adjustable-skip-list?
from: exact-integer?
to: exact-integer?
```

Increases the value of all keys greater than or equal to from by (- to from).

This operation takes time proportional to the number of elements with keys greater than or equal to from.

```
(skip-list-iterate-least/>? skip-list key)
→ (or/c skip-list-iter? #f)
 skip-list : skip-list?
 key : any/c
(skip-list-iterate-least/>=? skip-list key)
 → (or/c skip-list-iter? #f)
 skip-list : skip-list?
 key : any/c
(skip-list-iterate-greatest/<? skip-list
                               key)
 → (or/c skip-list-iter? #f)
 skip-list : skip-list?
 key : any/c
(skip-list-iterate-greatest/<=? skip-list</pre>
                                key)
 → (or/c skip-list-iter? #f)
 skip-list : skip-list?
 key : any/c
```

Implementations of dict-iterate-least, dict-iterate-greatest, dict-iterate-

least/>?, dict-iterate-least/>=?, dict-iterate-greatest/<?, and dictiterate-greatest/<=?, respectively.</pre>

```
(skip-list-iter? v) → boolean?
v : any/c
```

Returns #t if v represents a position in a skip-list, #f otherwise.

```
(skip-list-> list \ skip-list) \rightarrow (list of pair?)
skip-list : skip-list?
```

Returns an association list with the keys and values of skip-list, in order.

6 Interval Maps

```
(require data/interval-map)
```

An interval-map is a mutable data structure that maps *half-open* intervals of exact integers to values. An interval-map is queried at a discrete point, and the result of the query is the value mapped to the interval containing the point.

Internally, interval-maps use a splay-tree (data/splay-tree) of intervals for efficient query and update, including efficient contraction and expansion of intervals.

Interval-maps implement the dictionary (racket/dict) interface to a limited extent. Only dict-ref and the iteration-based methods (dict-iterate-first, dict-map, etc) are supported. For the iteration-based methods, the mapping's keys are considered the pairs of the start and end positions of the mapping's intervals.

Examples:

```
> (define r (make-interval-map))
> (interval-map-set! r 1 5 'apple)
> (interval-map-set! r 6 10 'pear)
> (interval-map-set! r 3 7 'banana)
> (dict-map r list)
'(((1 . 3) apple) ((3 . 7) banana) ((7 . 10) pear))
```

Makes a new empty interval-map.

```
(interval-map? v) \rightarrow boolean? v : any/c
```

Returns #t if v is an interval-map, #f otherwise.

Return the value associated with position in interval-map. If no mapping is found, default is applied if it is a procedure, or returned otherwise.

Updates interval-map, associating every position in [start, end) with value.

Existing interval mappings contained in [start, end) are destroyed, and partly overlapping intervals are truncated. See interval-map-update*! for an updating procedure that preserves distinctions within [start, end).

Updates interval-map, associating every position in [start, end) with the result of applying updater to the position's previously associated value, or to the default value produced by default if no mapping exists.

Unlike interval-map-set!, interval-map-update*! preserves existing distinctions within [start, end).

Removes the value associated with every position in [start, end).

Contracts interval-map's domain by removing all mappings on the interval [start, end) and decreasing intervals initally after end by (- end start).

If start is not less than end, an exception is raised.

Expands interval-map's domain by introducing a gap [start, end) and increasing intervals initially after start by (- end start).

If start is not less than end, an exception is raised.

```
(interval-map-cons*! interval-map
                        start
                        end
                       [default])
                                     \rightarrow void?
  interval-map : interval-map?
  start : any/c
  end : any/c
  v : any/c
  default : any/c = null
Same as the following:
  (interval-map-update*! interval-map start end
                           (lambda (old) (cons v old))
                           default)
(interval-map-iter? v) \rightarrow boolean?
  v : any/c
```

Returns #t if v represents a position in an interval-map, #f otherwise.

7 Binary Heaps

```
(require data/heap)
```

Binary heaps are a simple implementation of priority queues.

```
\frac{\text{(make-heap } <=?) \rightarrow \text{heap?}}{<=? : (-> \text{any/c any/c)}}
```

Makes a new empty heap using <=? to order elements.

```
\begin{array}{c}
\text{(heap? x)} \to \text{boolean?} \\
\text{x : any/c}
\end{array}
```

Returns #t if x is a heap, #f otherwise.

```
(heap-count h) → exact-nonnegative-integer?
h : heap?
```

Returns the number of elements in the heap.

Adds each v to the heap.

```
(heap-add-all! h \ v) \rightarrow void?

h : \text{heap}?

v : (\text{or/c list? vector? heap?})
```

Adds each element contained in v to the heap, leaving v unchanged.

```
\frac{\text{(heap-min }h) \rightarrow \text{any/c}}{\text{$h$ : heap?}}
```

Returns the least element in the heap h, according to the heap's ordering. If the heap is empty, an exception is raised.

Removes the least element in the heap h. If the heap is empty, an exception is raised.

```
(vector->heap <=? items) → heap?
<=?: (-> any/c any/c)
items: vector?
```

Builds a heap with the elements from items. The vector is not modified.

Returns a vector containing the elements of heap h in the heap's order. The heap is not modified.

```
(heap-copy h) → heap?
h : heap?
```

Makes a copy of heap h.

```
(heap-sort! <=? v) → void?
<=?: (-> any/c any/c)
v : vector?
```

Sorts vector v using the comparison function \leq =?.