# Typed Racket: Racket with Static Types

Version 5.1

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February 14, 2011

Typed Racket is a family of languages, each of which enforce that programs written in the language obey a type system that ensures the absence of many common errors. This guide is intended for programmers familiar with Racket. For an introduction to Racket, see the *Guide:* Racket.

# 1 Quick Start

Given a module written in the racket language, using Typed Racket requires the following steps:

- 1. Change the language to typed/racket.
- 2. Change the uses of (require mod) to (require typed/mod).
- 3. Annotate structure definitions and top-level definitions with their types.

Then, when the program is run, it will automatically be typechecked before any execution, and any type errors will be reported. If there are any type errors, the program will not run.

Here is an example program, written in the racket language:

```
#lang racket
  (define-struct pt (x y))

; mag : pt -> number
  (define (mag p)
        (sqrt (+ (sqr (pt-x p)) (sqr (pt-y p)))))

Here is the same program, in typed/racket:
  #lang typed/racket
  (define-struct: pt ([x : Real] [y : Real]))
  (: mag (pt -> Number))
  (define (mag p)
        (sqrt (+ (sqr (pt-x p)) (sqr (pt-y p)))))
```

# 2 Beginning Typed Racket

Recall the typed module from §1 "Quick Start":

```
#lang typed/racket
(define-struct: pt ([x : Real] [y : Real]))
(: mag (pt -> Number))
(define (mag p)
   (sqrt (+ (sqr (pt-x p)) (sqr (pt-y p)))))
```

Let us consider each element of this program in turn.

```
#lang typed/racket
```

This specifies that the module is written in the typed/racket language, which is a typed version of the racket language. Typed versions of other languages are provided as well; for example, the typed/racket/base language corresponds to racket/base.

```
(struct: pt ([x : Real] [y : Real]))
```

This defines a new structure, name pt, with two fields, x and y. Both fields are specified to have the type Real, which corresponds to the real numbers. The struct: form corresponds to the struct form from racket—when porting a program from racket to typed/racket, uses of struct should be changed to struct:.

Many forms in Typed Racket have the same name as the untyped forms, with a: suffix.

```
(: mag (pt -> Number))
```

This declares that mag has the type (pt -> Number).

The type (pt -> Number) is a function type, that is, the type of a procedure. The input type, or domain, is a single argument of type pt, which refers to an instance of the pt structure. The -> both indicates that this is a function type and separates the domain from the range, or output type, in this case Number.

```
(define (mag p)
   (sqrt (+ (sqr (pt-x p)) (sqr (pt-y p)))))
```

This definition is unchanged from the untyped version of the code. The goal of Typed Racket is to allow almost all definitions to be typechecked without change. The typechecker verifies that the body of the function has the type Real, under the assumption that p has the type pt, taking these types from the earlier type declaration. Since the body does have this type, the program is accepted.

### 2.1 Datatypes and Unions

Many data structures involve multiple variants. In Typed Racket, we represent these using *union types*, written (U t1 t2 ...).

In this module, we have defined two new datatypes: leaf and node. We've also defined the type name Tree to be (U node leaf), which represents a binary tree of numbers. In essence, we are saying that the tree-height function accepts a Tree, which is either a node or a leaf, and produces a number.

In order to calculate interesting facts about trees, we have to take them apart and get at their contents. But since accessors such as node-left require a node as input, not a Tree, we have to determine which kind of input we were passed.

For this purpose, we use the predicates that come with each defined structure. For example, the leaf? predicate distinguishes leafs from all other Typed Racket values. Therefore, in the first branch of the cond clause in tree-sum, we know that t is a leaf, and therefore we can get its value with the leaf-val function.

In the else clauses of both functions, we know that t is not a leaf, and since the type of t was Tree by process of elimination we can determine that t must be a node. Therefore, we can use accessors such as node-left and node-right with t as input.

### 2.2 Type Errors

When Typed Racket detects a type error in the module, it raises an error before running the program.

# Example:

```
> (add1 "not a number")
eval:2:0: Type Checker: Expected Complex, but got String
in: (quote "not a number")
```

# 3 Specifying Types

The previous section introduced the basics of the Typed Racket type system. In this section, we will see several new features of the language, allowing types to be specified and used.

### 3.1 Type Annotation and Binding Forms

In general, variables in Typed Racket must be annotated with their type.

#### 3.1.1 Annotating Definitions

We have already seen the : type annotation form. This is useful for definitions, at both the top level of a module

```
(: x Number)
(define x 7)
```

and in an internal definition

```
(let ()
  (: x Number)
  (define x 7)
  (add1 x))
```

In addition to the: form, almost all binding forms from racket have counterparts which allow the specification of types. The define: form allows the definition of variables in both top-level and internal contexts.

```
(define: x : Number 7)
(define: (id [z : Number]) : Number z)
```

Here, x has the type Number, and id has the type (Number -> Number). In the body of id, z has the type Number.

#### 3.1.2 Annotating Local Binding

```
(let: ([x : Number 7])
  (add1 x))
```

The let: form is exactly like let, but type annotations are provided for each variable bound. Here, x is given the type Number. The let\*: and letrec: are similar. Annotations are optional with let: and variants.

```
(let-values: ([([x : Number] [y : String]) (values 7 "hello")])
  (+ x (string-length y)))
```

The let\*-values: and letrec-values: forms are similar.

#### 3.1.3 Annotating Functions

Function expressions also bind variables, which can be annotated with types. This function expects two arguments, a Number and a String:

```
(lambda: ([x : Number] [y : String]) (+ x 5))
```

This function accepts at least one String, followed by arbitrarily many Numbers. In the body, y is a list of Numbers.

```
(lambda: ([x : String] . [y : Number *]) (apply + y))
```

This function has the type (String Number \* -> Number). Functions defined by cases may also be annotated:

This function has the type (case-lambda (-> Number) (Number -> Number)).

#### 3.1.4 Annotating Single Variables

When a single variable binding needs annotation, the annotation can be applied to a single variable using a reader extension:

```
(let ([#{x : Number} 7]) (add1 x))
```

This is equivalent to the earlier use of let:. This is especially useful for binding forms which do not have counterparts provided by Typed Racket, such as let+:

```
(let+ ([val #{x : Number} (+ 6 1)])
(* x x))
```

#### 3.1.5 Annotating Expressions

It is also possible to provide an expected type for a particular expression.

```
(ann (+ 7 1) Number)
```

This ensures that the expression, here (+ 7 1), has the desired type, here Number. Otherwise, the type checker signals an error. For example:

```
> (ann "not a number" Number)
eval:2:0: Type Checker: Expected Complex, but got String
in: (quote "not a number")
```

### 3.2 Type Inference

In many cases, type annotations can be avoided where Typed Racket can infer them. For example, the types of all local bindings using let and let\* can be inferred.

```
(let ([x 7]) (add1 x))
```

In this example, x has the type Exact-Positive-Integer.

Similarly, top-level constant definitions do not require annotation:

```
(define y "foo")
```

In this examples, y has the type String.

Finally, the parameter types for loops are inferred from their initial values.

```
(let loop ([x 0] [y (list 1 2 3)])
  (if (null? y) x (loop (+ x (car y)) (cdr y))))
```

Here x has the inferred type Integer, and y has the inferred type (Listof Integer). The loop variable has type (Integer (Listof Integer) -> Integer).

### 3.3 New Type Names

Any type can be given a name with define-type.

```
(define-type NN (Number -> Number))
```

Anywhere the name NN is used, it is expanded to (Number -> Number). Type names may not be recursive.

# 4 Types in Typed Racket

Typed Racket provides a rich variety of types to describe data. This section introduces them.

### 4.1 Basic Types

The most basic types in Typed Racket are those for primitive data, such as True and False for booleans, String for strings, and Char for characters.

```
> '"hello, world"
- : String
"hello, world"
> #\f
- : Char
#\f
> #t
- : True
#t
> #f
```

Each symbol is given a unique type containing only that symbol. The Symbol type includes all symbols.

```
> 'foo
- : 'foo
'foo
> 'bar
- : 'bar
'bar
```

Typed Racket also provides a rich hierarchy for describing particular kinds of numbers.

```
> 0
- : Zero
0
> -7
- : Negative-Fixnum
-7
> 14
- : Positive-Fixnum
14
> 3.2
- : Nonnegative-Float
3.2
```

```
> 7.0+2.8i
- : Float-Complex
7.0+2.8i
```

Finally, any value is itself a type:

```
> (ann 23 : 23)
- : 23
23
```

#### **4.2** Function Types

We have already seen some examples of function types. Function types are constructed using ->, with the argument types before the arrow and the result type after. Here are some example function types:

```
(Number -> Number)
(String String -> Boolean)
(Char -> (values String Natural))
```

The first type requires a Number as input, and produces a Number. The second requires two arguments. The third takes one argument, and produces multiple values, of types String and Natural. Here are example functions for each of these types.

### 4.3 Union Types

Sometimes a value can be one of several types. To specify this, we can use a union type, written with the type constructor U.

```
- : (U 'no 'yes)
'no
```

Any number of types can be combined together in a union, and nested unions are flattened.

```
(U Number String Boolean Char)
```

### 4.4 Recursive Types

*Recursive types* can refer to themselves. This allows a type to describe an infinite family of data. For example, this is the type of binary trees of numbers.

```
(define-type BinaryTree (Rec BT (U Number (Pair BT BT))))
```

The Rec type constructor specifies that the type BT refers to the whole binary tree type within the body of the Rec form.

#### 4.5 Structure Types

Using struct: introduces new types, distinct from any previous type.

```
(struct: point ([x : Real] [y : Real]))
```

Instances of this structure, such as (point 7 12), have type point.

#### 4.6 Subtyping

In Typed Racket, all types are placed in a hierarchy, based on what values are included in the type. When an element of a larger type is expected, an element of a smaller type may be provided. The smaller type is called a *subtype* of the larger type. The larger type is called a *supertype*. For example, Integer is a subtype of Real, since every integer is a real number. Therefore, the following code is acceptable to the type checker:

```
(: f (Real -> Real))
(define (f x) (* x 0.75))
(: x Integer)
(define x -125)
(f x)
```

All types are subtypes of the Any type.

The elements of a union type are individually subtypes of the whole union, so String is a subtype of (U String Number). One function type is a subtype of another if they have the same number of arguments, the subtype's arguments are more permissive (is a supertype), and the subtype's result type is less permissive (is a subtype). For example, (Any -> String) is a subtype of (Number -> (U String #f)).

### 4.7 Polymorphism

Typed Racket offers abstraction over types as well as values.

#### 4.7.1 Polymorphic Data Structures

Virtually every Racket program uses lists and other collections. Fortunately, Typed Racket can handle these as well. A simple list processing program can be written like this:

```
#lang typed/racket
(: sum-list ((Listof Number) -> Number))
(define (sum-list 1)
  (cond [(null? 1) 0]
        [else (+ (car 1) (sum-list (cdr 1)))]))
```

This looks similar to our earlier programs — except for the type of 1, which looks like a function application. In fact, it's a use of the *type constructor* Listof, which takes another type as its input, here Number. We can use Listof to construct the type of any kind of list we might want.

We can define our own type constructors as well. For example, here is an analog of the Maybe type constructor from Haskell:

```
#lang typed/racket
(struct: None ())
(struct: (a) Some ([v : a]))

(define-type (Opt a) (U None (Some a)))

(: find (Number (Listof Number) -> (Opt Number)))
(define (find v 1)
        (cond [(null? 1) (None)]
        [(= v (car 1)) (Some v)]
        [else (find v (cdr 1))]))
```

The first struct: defines None to be a structure with no contents.

The second definition

```
(struct: (a) Some ([v : a]))
```

creates a parameterized type, Some, which is a structure with one element, whose type is that of the type argument to Some. Here the type parameters (only one, a, in this case) are written before the type name, and can be referred to in the types of the fields.

The type definiton

```
(define-type (Opt a) (U None (Some a)))
```

creates a parameterized type — Opt is a potential container for whatever type is supplied.

The find function takes a number v and list, and produces (Some v) when the number is found in the list, and (None) otherwise. Therefore, it produces a (Opt Number), just as the annotation specified.

#### 4.7.2 Polymorphic Functions

Sometimes functions over polymorphic data structures only concern themselves with the form of the structure. For example, one might write a function that takes the length of a list of numbers:

and also a function that takes the length of a list of strings:

Notice that both of these functions have almost exactly the same definition; the only difference is the name of the function. This is because neither function uses the type of the elements in the definition.

We can abstract over the type of the element as follows:

```
#lang typed/racket
(: list-length (All (A) ((Listof A) -> Integer)))
```

The new type constructor All takes a list of type variables and a body type. The type variables are allowed to appear free in the body of the All form.

### 4.8 Variable-Arity Functions: Programming with Rest Arguments

Typed Racket can handle some uses of rest arguments.

#### 4.8.1 Uniform Variable-Arity Functions

In Racket, one can write a function that takes an arbitrary number of arguments as follows:

The arguments to the function that are in excess to the non-rest arguments are converted to a list which is assigned to the rest parameter. So the examples above evaluate to 0, 10, and 4.

We can define such functions in Typed Racket as well:

This type can be assigned to the function when each element of the rest parameter is used at the same type.

#### 4.8.2 Non-Uniform Variable-Arity Functions

However, the rest argument may be used as a heterogeneous list. Take this (simplified) definition of the Racket function map:

Here the different lists that make up the rest argument bss can be of different types, but the type of each list in bss corresponds to the type of the corresponding argument of f. We also know that, in order to avoid arity errors, the length of bss must be one less than the arity of f (as as corresponds to the first argument of f).

```
The example uses of map evaluate to (list 2 3 4 5), (list (list 1 4) (list 2 5) (list 3 6)), and (list 10 14 18).
```

In Typed Racket, we can define map as follows:

Note that the type variable B is followed by an ellipsis. This denotes that B is a dotted type variable which corresponds to a list of types, much as a rest argument corresponds to a list of values. When the type of map is instantiated at a list of types, then each type t which is bound by B (notated by the dotted pre-type t ... B) is expanded to a number of copies of t equal to the length of the sequence assigned to B. Then B in each copy is replaced with the corresponding type from the sequence.

```
So the type of (inst map Integer Boolean String Number) is

((Boolean String Number -> Integer) (Listof Boolean) (Listof String)
(Listof Number) -> (Listof Integer)).
```

# 5 Optimization in Typed Racket

Typed Racket provides a type-driven optimizer that rewrites well-typed programs to potentially make them faster. It should in no way make your programs slower or unsafe.

### 5.1 Turning the optimizer off

Typed Racket's optimizer is turned on by default. If you want to deactivate it (for debugging, for instance), you must add the #:no-optimize keyword when specifying the language of your program:

```
#lang typed/racket #:no-optimize
```

#### 5.2 Getting the most out of the optimizer

Typed Racket's optimizer can improve the performance of various common Racket idioms. However, it does a better job on some idioms than on others. By writing your programs using the right idioms, you can help the optimizer help you.

#### 5.2.1 Numeric types

Being type-driven, the optimizer makes most of its decisions based on the types you assigned to your data. As such, you can improve the optimizer's usefulness by writing informative types.

For example, the following programs both typecheck:

```
(define: (f (x : Real)) : Real (+ x 2.5))
(f 3.5)
(define: (f (x : Float)) : Float (+ x 2.5))
(f 3.5)
```

However, the second one uses more informative types: the Float type includes only 64-bit floating-point numbers whereas the Real type includes both exact and inexact real numbers and the Inexact-Real type includes both 32- and 64-bit floating-point numbers. Typed Racket's optimizer can optimize the latter program to use float -specific operations whereas it cannot do anything with the former program.

Thus, to get the most of Typed Racket's optimizer, you should use the Float type when possible. For similar reasons, you should use floating-point literals instead of exact literals

when doing floating-point computations.

When mixing floating-point numbers and exact reals in arithmetic operations, the result is not necessarily a Float. For instance, the result of (\* 2.0 0) is 0 which is not a Float. This can result in missed optimizations. To prevent this, when mixing floating-point numbers and exact reals, coerce exact reals to floating-point numbers using exact->inexact. This is not necessary when using + or -. When mixing floating-point numbers of different precisions, results use the highest precision possible.

On a similar note, the Float-Complex type is preferable to the Complex type for the same reason. Typed Racket can keep inexact complex numbers unboxed; as such, programs using complex numbers can have better performance than equivalent programs that represent complex numbers as two real numbers. As with floating-point literals, inexact complex literals (such as 1.0+1.0i) should be preferred over exact complex literals (such as 1+1i). Note that both parts of a literal must be present and inexact for the literal to be of type Float-Complex; 0.0+1.0i is of type Float-Complex but 0+1.0i is not. To get the most of Typed Racket's optimizer, you should also favor rectangular coordinates over polar coordinates.

#### **5.2.2** Lists

Typed Racket handles potentially empty lists and lists that are known to be non-empty differently: when taking the car or the cdr of a list Typed Racket knows is non-empty, it can skip the check for the empty list that is usually done when calling car and cdr.

In this example, Typed Racket knows that if we reach the else branch, 1 is not empty. The checks associated with car and cdr would be redundant and are eliminated.

In addition to explicitly checking for the empty list using null?, you can inform Typed Racket that a list is non-empty by using the known-length list type constructor; if your data is stored in lists of fixed length, you can use the List type constructors.

For instance, the type of a list of two Integers can be written either as:

```
(define-type List-2-Ints (Listof Integer))
or as the more precise:
  (define-type List-2-Ints (List Integer Integer))
```

Using the second definition, all car and cdr-related checks can be eliminated in this function:

```
(define: (sum2 (1 : List-2-Ints) : Integer)
  (+ (car 1) (car (cdr 1))))
```

#### 5.2.3 Vectors

In addition to known-length lists, Typed Racket supports known-length vectors through the Vector type constructor. Known-length vector access using constant indices can be optimized in a similar fashion as car and cdr.

```
; #(name r g b)
(define-type Color (Vector String Integer Integer Integer))
(define: x : Color (vector "red" 255 0 0))
(vector-ref x 0) ; good
(define color-name 0)
(vector-ref x color-name) ; good
(vector-ref x (* 0 10)) ; bad
```